

## BINARY CODED DECIMAL ADDITION

### Field of the invention

The present invention relates to a binary coded decimal (BCD) addition, including an  
5 adder circuit.

### Background

In BCD arithmetic, at least four binary bits are needed to represent the numbers from 0 to 9. There are sixteen possible bit combinations using four binary bits, but only ten (i.e., 0  
10 to 9) are valid BCD digits. Traditionally, BCD adder circuits adjust the binary sum after the addition has been completed if the value is more than nine (i.e.,  $1001_2$ ). For example, whenever the unadjusted sum of two BCD digits produced a carry out (i.e., when the sum exceeds  $1001_2$ ), the sum is corrected by adding  $0110_2$ .

A known BCD adder, described in "Logic and Computer Design Fundamentals", M  
15 Morris Mano and Charles R Kime, Pearson Educational Asia, second edition, 2001 is shown in **Fig. 1**. The BCD adder circuit 5 uses a four-bit binary adder 6 to add two BCD operands **A(3)** to **A(0)** and **B(3)** to **B(0)**, and an input carry **C<sub>in</sub>** to produce an intermediate sum **Z(3)** to **Z(0)**. The adder circuit 6 also includes two levels of logic gates 7, 8, 9 to calculate the BCD carry output **Cout** from the intermediate sum. If there is a BCD carry,  
20 a correction factor of  $0110_2$  is added with the intermediate sum using a further binary adder 10.

The BCD adder circuit 5 shown in **Fig. 1** thus uses 10 levels of gates to perform a 4-bit addition. For a 16-bit adder circuit, the corresponding binary adder circuit requires 16 levels of gates. However the critical path is the generation of the carry **Cout**, and gate  
25 levels required to implement this is 22 for 16-bit BCD addition.

Another BCD adder circuit is taught in US Patent No. 4,805,131 (Adlietta et al, assigned to Digital Equipment Corporation), issued on February 14, 1989. The BCD adder of Adlietta et al has three stages. In the first stage,  $0110_2$  is added with the input BCD  
30 operands without considering the input carry. In the second stage the sum and carry vectors are added using a carry look ahead network to generate final carry and propagate vectors. In the third stage a correction circuit adds  $1010_2$  if needed.

The logic terms in the calculation of a FINAL\_CARRY vector increases as the number of bits of the BCD operands increases. Also, the carry vector calculated is propagated through every bit position. The bit terms of the FINAL\_CARRY vector must propagate through every bit position. As the bit position increases from least significant bit position

- 5 0 through most significant bit position 15, the number of logical terms required to produce the terms of the FINAL\_CARRY vector also increases. Therefore, more sophisticated logic gates are required to produce the more significant bit terms and keep the number of logic levels and associated delay to a minimum.

For 16-bit BCD addition the BCD adder circuit of Adlietta et al uses only 12 gate levels

- 10 compared to 22 gate levels in the BCD adder circuit of Fig. 1. But the logic terms required for the implementation of the FINAL\_CARRY of BCD adder of Adlietta et al is much higher. Also, when the number of bits of the BCD operands increase, the logic terms for calculating the FINAL\_CARRY also increases, which makes the implementation complex for more than 16-bits. There also is no reusability, meaning 15 extending similar structures when the number of bits of the input BCD operands increases.

There remains a need for BCD addition circuits with lesser a number of gate levels as well as lesser number of logic terms without requiring any sophisticated logic gates.

There is also a need to increase the reusability of logic gates in such adders.

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### **Summary**

The binary coded decimal (BCD) adder circuit adds two BCD encoded operands, with an input carry bit, and produces a BCD encoded sum. The adder includes three stages. The first stage receives two BCD encoded operands as inputs, groups the inputs into

- 25 contiguous blocks of 4-bits each, computes an intermediate sum vector and carry vector without considering the input carry bit, and also computes propagation and generate functions for each 4-bit group. The second stage is a carry look ahead circuit which computes all carries from the input carry, and the propagate and generate functions of the 4-bit groups from the first stage. The third stage adjusts the intermediate sum vector with, 30 pre-correction factors which depend upon the input carry and the carries generated from the second stage and the carry vectors from the first stage.

This invention reduces the time required to perform a BCD addition by reducing in the number of gate levels of the critical path for adding two BCD operands of 16-bits each with an input carry to 12. Only 15 gate levels of delay arise for adding two 64-bit BCD encoded operands with an input carry. The gate levels thus increase only by three, from  
5 twelve to fifteen, when the input BCD operands bit size increases from sixteen to sixty-four.

Since the BCD addition is carried out with 4-bit groups, the same logic structure can be extended to provide a 16-, 32- or 64-bit BCD adder with extra levels of carry look ahead circuit, which increases the reusability of the logic.

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#### **Description of drawings**

**Fig. 1** shows a known BCD adder circuit.

**Fig. 2** shows a 16-bit BCD adder circuit embodying the invention.

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**Fig. 3** shows detail of the circuit of **Fig. 2** when an addition of a first group of bits is performed.

**Fig. 4** shows a circuit for calculating first intermediate sum and carry vectors.

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**Fig. 5** shows a circuit for calculating second intermediate sum and carry vectors.

**Fig. 6** shows a circuit for calculating third intermediate sum and carry vectors.

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**Fig. 7** shows a carry look ahead circuit.

**Fig. 8** shows a circuit for performing a SUM(0) correction.

**Fig. 9** shows a circuit for performing a SUM(1) correction.

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**Fig. 10** shows a circuit for performing a SUM(2) correction.

**Fig. 11** shows a circuit for performing a SUM(3) correction.

**Fig. 12** shows a stage 1 circuit for a 64-bit BCD adder circuit.

**Fig. 13** shows a carry look ahead circuit for the 64-bit BCD adder circuit.

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**Fig. 14** shows a sum correction circuit for the 64-bit BCD adder circuit.

### Detailed description

#### Overview

- 10 The BCD addition of two operands each of n bits with an input carry bit will be described with reference to **Fig. 2**. A BCD adder circuit **12** generally has three stages, and the number of bits of the operands is n=16. The addition is performed after grouping the n-bits into contiguous (or successive) groups of 4-bits (i.e., bits 0-3, bits 4-7, bits 8-11, bits 12-15).
- 15 The first stage, represented by four circuits **13**, **14**, **15**, **16**, generates intermediate sum and carry vectors and propagate and generate functions. The second stage has a carry look ahead circuit **17** to generate carries from the input carry, and the propagate and generate functions from the first stage. The third stage includes four circuits **18**, **19**, **20**, **21** that generate a final sum from the intermediate sum vectors based on pre-correction factors
- 20 which depend on the input carry and the carries generated from carry look ahead circuit **17** and first stage circuits **13**, **14**, **15**, **16**.

#### First stage

Consider the 16-bit BCD addition of two BCD encoded operands **A(15)** to **A(0)** and **B(15)** to **B(0)**.

- 25 The addition of first group of 4-bits **A(3)** to **A(0)** and **B(3)** to **B(0)** by the circuit **13** is explained with reference to **Figs. 3, 4, 5 and 6**. The circuits **14**, **15**, **16** for the other three groups of 4-bit addition logic are of the same form.

As shown in **Fig. 3**, three intermediate sum vectors **FS[3:0]**, **SS[3:0]**, and **TS[3:0]**, (where “F” = first, “S” = second and “T” = third) and carry vectors **FC[4:0]**, **SC[3:0]**,

- 30 **TC3** to **TC0** are calculated by sequential generator circuits **22**, **23**, **24**. The third sum and

carry vectors **TS[3:0]** and **TC3** to **TC0** are provided to a respective sum correction circuit **18** of the third stage.

The circuit **22** computes the first intermediate sum vector **FS(3)** to **FS(0)** and carry vector **FC(4)** to **FC(1)** by Half-Adders (XOR and AND gates) as shown in **Fig. 4**. The logical

5 operations performed are:

$$\mathbf{FS(3)} = \mathbf{A(3)} \text{ XOR } \mathbf{B(3)} \quad (\text{gate 37})$$

$$\mathbf{FS(2)} = \mathbf{A(2)} \text{ XOR } \mathbf{B(2)} \quad (\text{gate 35})$$

$$\mathbf{FS(1)} = \mathbf{A(1)} \text{ XOR } \mathbf{B(1)} \quad (\text{gate 33})$$

$$\mathbf{FS(0)} = \mathbf{A(0)} \text{ XOR } \mathbf{B(0)} \quad (\text{gate 31})$$

10       $\mathbf{FC(4)} = \mathbf{A(3)} \text{ AND } \mathbf{B(3)} \quad (\text{gate 38})$

$$\mathbf{FC(3)} = \mathbf{A(2)} \text{ AND } \mathbf{B(2)} \quad (\text{gate 36})$$

$$\mathbf{FC(2)} = \mathbf{A(1)} \text{ AND } \mathbf{B(1)} \quad (\text{gate 34})$$

$$\mathbf{FC(1)} = \mathbf{A(0)} \text{ AND } \mathbf{B(0)} \quad (\text{gate 32})$$

$$\mathbf{FC(0)} = '0'$$

15      The second intermediate sum vector of the first stage **SS(3)** to **SS(0)** and carry vector **SC(3)** to **SC(2)** are calculated by the circuit **23**, including Half-Adders, as shown in detail in **Fig. 5**. The logical operations performed are:

$$\mathbf{SS(3)} = \mathbf{FS(3)} \text{ XOR } \mathbf{FC(3)} \quad (\text{gate 43})$$

$$\mathbf{SS(2)} = \mathbf{FS(2)} \text{ XOR } \mathbf{FC(2)} \quad (\text{gate 41})$$

20       $\mathbf{SS(1)} = \mathbf{FS(1)} \text{ XOR } \mathbf{FC(1)} \quad (\text{gate 39})$

$$\mathbf{SS(0)} = \mathbf{FS(0)} \text{ XOR } \mathbf{FC(0)} = \mathbf{FS(0)}; \text{ since } \mathbf{FC(0)} = '0'$$

$$\mathbf{SC(3)} = \mathbf{FS(2)} \text{ AND } \mathbf{FC(2)} \quad (\text{gate 42})$$

$$\mathbf{SC(2)} = \mathbf{FS(1)} \text{ AND } \mathbf{FC(1)} \quad (\text{gate 40})$$

**SC(1) = FS(0) AND '0' = '0'; since FC(0) = '0'**

**SC(0) = '0'**

The third intermediate sum vectors of the first stage **TS(3)** to **TS(0)** and a carry **TC3** are calculated by the circuit 24, including Half-Adders, as shown in detail in Fig. 6. The  
5 logical operations performed are:

**TS(3) = SS(3) XOR SC(3)** (gate 46)

**TS(2) = SS(2) XOR SC(2)** (gate 44)

**TS(1) = SS(1) XOR SC(1) = SS(1); since SC(1) = '0'**

**TS(0) = SS(0) XOR SC(0) = FS(0); since SC(0) = '0' and SS(0) = FS(0)**

10 **TC3 = SS(2) AND SC(2)** (gate 45)

**TC2 = SS(1) AND SC(1) = '0'; since SC(1) = '0'**

**TC1 = SS(0) AND SC(0) = '0'; since SC(0) = '0'**

**TC0 = '0'**

Comparing Figs. 4-6, it can be seen that the design has been optimized such that Half-  
15 Adder circuits reduce to XOR gates or even to being straight through in some instances.

The propagate function **P3-0** and the generate function **G3-0** for the first group of 4-bits are calculated from the intermediate sum and carry vectors, by the combination logic shown in Fig. 3 represented by gates 25, 26, 27, 28, 29, 30. The logical operations performed are:

20 **P3-0 = TS(3) AND TS(0)** (gate 30)

**G3-0 = ( SS(1) AND (SS(3) OR SC(3)) ) OR ( SS(3) AND (SS(2) OR SC(2)) ) OR FC(4)** (gates 25, 26, 27, 28, 29)

Thus the functions **P3-0** and **G3-0**, along with other 4-bit group propagate and generate functions **P7-4, P11-8, P15-12, G7-4, G11-8** and **G15-12**, are inputs to the second stage  
25 carry look ahead circuit 17.

### *Second stage*

The second stage carry look ahead circuit 17, calculates the carry values of all groups of 4-bits from the propagate and generate values of the first stage and the input carry bit C0 as shown in Fig. 7.

These carries are provided to the third stage.

The carry **C16** will be calculated only for a 16-bit BCD addition. If 32-bit or 64-bit BCD addition is required, then propagate function **P15-0** and generate function **G15-0** will be produced instead of **C16** to be provided as an input to the 64-bit carry look ahead network, shown in Fig. 13. The propagate and generate functions **P15-0** and **G15-0** are calculated as:

**P15-0 = P15-12 AND P11-8 AND P7-4 AND P3-0**

20      **G15-0 = G15-12 OR (P15-12 AND G11-8) OR (P15-12 AND P11-8 AND G7-4)**  
          **OR (P15-12 AND P11-8 AND P7-4 AND G3-0)**

The values **P3-0**, **P7-4**, **P11-8** and **P15-12** are propagate functions and **G3-0**, **G7-4**, **G11-8** and **G15-12** are generate functions from the first stage circuits **13,14,15** and **16** of Fig. **2**.

25 *Third stage*

The third stage circuits **18, 19, 20, 21** adjust the sum with pre-correction factors which depend on the carries generated from the first stage circuits **13, 14, 15, 16**, the second stage carry look ahead circuit **17** and, in one case, the input carry **C0**.

- In general, the sum correction for a 4-bit block(say N down to N-3) adds first stage 4-bit
- 5      sum vector **TS[N:N-3]** and a pre-correction factor. The pre-correction factor is one of the values of  $(TC_N000)_2$  or  $(TC_N001)_2$  or  $(TC_N110)_2$  or  $(TC_N111)_2$  which will be decided based on the carry  $C_{N-3}$  of previous 4-bits(N-4 down to N-7) and the carry  $C_{N+1}$  of current 4 bits(N down to N-3).

For example, the general steps for sum correction block of bits 7 to 4 (where N = 7) are:

10      Step 1

One of the values "TC<sub>7</sub> 0 0 0", "TC<sub>7</sub> 0 0 1", "TC<sub>7</sub> 1 1 0", "TC<sub>7</sub> 1 1 1" will be selected by C8 (Carry for bits 7 to 4) and C4 (carry of previous 4 bits i.e. bits 3 to 0).

if C8=0 and C4=0 => selection of TC<sub>7</sub>000. (TC<sub>7</sub> is a single bit having value '1' or '0')

15      if C8=0 and C4=1 => selection of TC<sub>7</sub>001

if C8=1 and C4=0 => selection of TC<sub>7</sub>110

if C8=1 and C4=1 => selection of TC<sub>7</sub>111

Step 2

The above selected value will be added with first stage SUM vector **TS[N:N-3]**.

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The first of the 4-bit group sum correction circuits, namely circuit **18**, will now be explained in detail.

- 25      The inputs to the sum correction circuit **18** are the third intermediate sum vectors **TS(3)** to **TS(0)**, the intermediate carry **TC3** from the first stage the input carry **C0** and the carry **C4** from the second stage carry look ahead circuit **17**.

If the Pre-correction Factor (PF) is taken as **PF(3)** to **PF(0)**, and the intermediate sum is **TS(3)** to **TS(0)**, then the Final Sum will be obtained from the following steps, which have four levels of calculations.

In the first level, a First Correction Sum vector **FCS** and a First Correction Carry vector **FCC** are calculated from the PF vector (**PF(3)** to **PF(0)**) and the TS vector (**TS(3)** to **TS(0)**) as shown in **Table 1**.

5	First_Correction_Sum	First_Correction_Carry
	-----	-----
	<b>FCS(3) = TS(3) XOR PF(3)</b>	<b>FCC(3) = TS(2) AND PF(2)</b>
	<b>FCS(2) = TS(2) XOR PF(2)</b>	<b>FCC(2) = TS(1) AND PF(1)</b>
	<b>FCS(1) = TS(1) XOR PF(1)</b>	<b>FCC(1) = TS(0) AND PF(0)</b>
10	<b>FCS(0) = TS(0) XOR PF(0)</b>	<b>FCC(0) = '0'</b>

**TABLE 1**

In the second level, a Second Correction Sum **SCS** and a Second Correction Carry **SCC** are calculated from first level outputs **FCS(3)** to **FCS(0)** and **FCC(3)** to **FCC(0)** as  
15 shown in **Table 2**.

	Second_Correction_Sum	Second_Correction_Carry
	-----	-----
	<b>SCS(3) = FCS(3) XOR FCC(3)</b>	<b>SCC(3) = FCS(2) AND FCC(2)</b>
20	<b>SCS(2) = FCS(2) XOR FCC(2)</b>	<b>SCC(2) = FCS(1) AND FCC(1)</b>
	<b>SCS(1) = FCS(1) XOR FCC(1)</b>	<b>SCC(1) = FCS(0) AND FCC(0)</b>
	<b>SCS(0) = FCS(0) XOR FCC(0)</b>	<b>SCC(0) = '0'</b>

**TABLE 2**

In the third level, a Third Correction Sum **TCS** and Third Correction Carry **TCC** are calculated from second level outputs **SCS(3)** to **SCS(0)** and **SCC(3)** to **SCC(0)** as shown in **Table 3**.

5	Third_Correction_Sum	Third_Correction_Carry
	-----	-----
	<b>TCS(3) = SCS(3) XOR SCC(3)</b>	<b>TCC(3) = SCS(2) AND SCC(2)</b>
	<b>TCS(2) = SCS(2) XOR SCC(2)</b>	<b>TCC(2) = SCS(1) AND SCC(1)</b>
	<b>TCS(1) = SCS(1) XOR SCC(1)</b>	<b>TCC(1) = SCS(0) AND SCC(0)</b>
10	<b>TCS(0) = SCS(0) XOR SCC(0)</b>	<b>TCC(0) = '0'</b>

**TABLE 3**

In the fourth level, a final SUM vector is calculated from the third level outputs **TCS(3)** to **TCS(0)** and **TCC(3)** to **TCC(0)** as shown in **Table 4**.

15	Final_Sum
	-----
	<b>SUM(3) = TCS(3) XOR TCC(3)</b>
	<b>SUM(2) = TCS(2) XOR TCC(2)</b>
	<b>SUM(1) = TCS(1) XOR TCC(1)</b>
	<b>SUM(0) = TCS(0) XOR TCC(0)</b>

**TABLE 4**

As mentioned, the Pre-correction Factor **PF(3)** to **PF(0)** is, in part, dependent upon the carries **C0** and **C4**. The Pre-correction Factor **PF(3)** to **PF(0)** is given below for each of four cases:

If the **C4** = '0' and **C0** = '0', the **PF(3)** to **PF(0)** is (TC3 0 0 0)-----Case1

If the **C4** = '0' and **C0** = '1', the **PF(3)** to **PF(0)** is (TC3 0 0 1)-----Case2

If the **C4** = '1' and **C0** = '0', the **PF(3)** to **PF(0)** is (TC3 1 1 0)-----Case3

If the **C4** = '1' and **C0** = '1', the **PF(3)** to **PF(0)** is (TC3 1 1 1)-----Case4

## 5 Case 1

The final SUM vector is obtained after substituting **PF(3)** to **PF(0)** values (TC3 0 0 0) in the First\_Sum\_Correction and First\_Carry\_Correction equations and then reducing the Second\_Sum\_Correction, Second\_Carry\_Correction, Third\_Sum\_Correction and Third\_Carry\_Correction equations. The finally reduced SUM vector is given below:

10      **SUM(3) = TS(3) XOR TC3** ----- equ03

**SUM(2) = TS(2)** ----- equ02

**SUM(1) = TS(1)** ----- equ01

**SUM(0) = TS(0)** ----- equ00

## Case 2

15      The final SUM vector is obtained after substituting **PF(3)** to **PF(0)** values (TC3 0 0 1) in the First\_Sum\_Correction and First\_Carry\_Correction equations and then reducing the Second\_Sum\_Correction, Second\_Carry\_Correction, Third\_Sum\_Correction and Third\_Carry\_Correction equations. The finally reduced SUM vector is given below:

**SUM(3) = TS(3) XOR TC3 XOR (TS(0) AND TS(1) AND TS(2))** -----equ13

20      **SUM(2) = ( TS(0) AND TS(1) ) XOR TS(2)** -----equ12

**SUM(1) = TS(0) XOR TS(1)** -----equ11

**SUM(0) = NOT TS(0)** -----equ10

## Case 3

25      The final SUM vector is obtained after substituting **PF(3)** to **PF(0)** values (TC3 1 1 0) in the First\_Sum\_Correction and First\_Carry\_Correction equations and then reducing the

Second\_Sum\_Correction, Second\_Carry\_Correction, Third\_Sum\_Correction and Third\_Carry\_Correction equations. The finally reduced SUM vector is given below:

$$\text{SUM}(3) = \text{TS}(3) \text{ XOR } \text{TC}3 \text{ XOR } (\text{TS}(1) \text{ OR } \text{TS}(2)) \quad \text{-----equ23}$$

$$\text{SUM}(2) = \text{TS}(1) \text{ XOR } (\text{NOT TS}(2)) \quad \text{-----equ22}$$

5             $\text{SUM}(1) = \text{NOT TS}(1) \quad \text{-----equ21}$

$\text{SUM}(0) = \text{TS}(0) \quad \text{-----equ20}$

#### Case 4

The final SUM vector is obtained after substituting **PF(3)** to **PF(0)** values (TC3 1 1 1) in the First\_Sum\_Correction and First\_Carry\_Correction equations and then reducing the

10          Second\_Sum\_Correction, Second\_Carry\_Correction, Third\_Sum\_Correction and Third\_Carry\_Correction equations. The finally reduced SUM vector is given below

$$\text{SUM}(3) = \text{TS}(3) \text{ XOR } \text{TC}(3) \text{ XOR } (\text{TS}(0) \text{ OR } \text{TS}(1) \text{ OR } \text{TS}(2)) \quad \text{-----equ33}$$

$$\text{SUM}(2) = (\text{TS}(0) \text{ OR } \text{TS}(1)) \text{ XOR } (\text{NOT TS}(2)) \quad \text{-----equ32}$$

$$\text{SUM}(1) = \text{TS}(0) \text{ XOR } (\text{NOT TS}(1)) \quad \text{-----equ31}$$

15           $\text{SUM}(0) = \text{NOT TS}(0) \quad \text{-----equ30}$

The implementation of **SUM(0)** correction circuit from equ00, equ10, equ20 and equ30 is shown in **FIG. 8**. The implementation of **SUM(1)** correction circuit from equ01, equ11,

equ21 and equ31 is shown in **Fig. 9**. The implementation of **SUM(2)** correction circuit

from equ02, equ12, equ22 and equ32 is shown in **Fig. 10**. The implementation of

20          **SUM(3)** correction circuit from equ03, equ13, equ23 and equ33 is shown in **Fig. 11**.

Clearly, there are equivalent circuits to those shown in **Figs. 8-11** for each of the other sum correction circuits **19, 20, 21**, to generate **SUM[7:4]**, **SUM[11:8]**, and **SUM[15:12]** values.

#### *Final Sum*

25          The Final Sum of the BCD addition is the sequence of **SUM[15:12]**, **SUM[11:8]**, **SUM[7:4]**, **SUM [3:0]**. A final carry, equal to **C16**, also results as an output.

### *Critical Paths*

In the BCD addition circuit **12** as described, there are a number of critical paths in the three stages. Critical paths determine the number of logic levels required, and the speed at which addition can be performed.

**5** Critical paths in the first stage:

CRITICAL\_PATH\_1 - The path through circuits **22**, **23** and **24** which generates intermediate sum vector **TS(3)** to **TS(0)** from the BCD input operands **A(3)** to **A(0)** and **B(3)** to **B(0)** contains three XOR gates, and so the gate levels for this critical path is considered as 6.

- 10** CRITICAL\_PATH\_2a - The path through circuits **22**, **23** and gates **26**, **28**, **30** from the BCD input operands to the generate function requires 7 gate levels.

CRITICAL\_PATH\_2b - The path through circuits **22**, **23** and gates **25**, **27**, **30** from the BCD input operands to the generate function requires 7 gate levels.

- 15** CRITICAL\_PATH\_2c - The path through circuits **22**, **23**, **24** and gate **29** from the BCD input operands to the propagate function requires 7 gate levels.

### Critical paths in the second stage:

CRITICAL\_PATH\_3 - The carry look ahead circuit for 16-bit BCD addition (circuit **17** in Fig. 3) requires two gate levels of logic.

### Critical paths in the third stage:

- 20** CRITICAL\_PATH\_4 - The SUM correction circuit's critical path (gates **77**, **78** and MUX **81** of Fig.11) from first stage output intermediate sum vector to final SUM vector requires 6 levels of gates, of which 4 levels are calculated before receiving the carries from the carry look ahead circuit **17**.

- 25** CRITICAL\_PATH\_5 - The path from the carry look ahead output carries to the final SUM which has 2 gate levels (MUX **62** or MUX **66** or MUX **73** or MUX **81**).

In the case of the 16-bit BCD adder circuit, the critical path is through SUM correction circuit and the path is CRITICAL\_PATH\_1 (6 gate levels) + CRITICAL\_PATH\_4 (6 gate levels). So the 16-bit BCD adder circuit has a delay of only 12 gate levels.

In the case of a 64-bit or 32 bits BCD adder circuit, the critical path is through the Carry look ahead circuit and the path is CRITICAL\_PATH\_2a or CRITICAL\_PATH\_2b or CRITICAL\_PATH\_2c (all are 7 gate levels) + CRITICAL\_PATH\_3 (6 gate levels) + CRITICAL\_PATH\_5 (2 gate levels). Therefore, 64-bit or 32-bit BCD adder circuits have

- 5 15 gate levels of logic in the critical path.

*The 64-Bit adder circuit*

The 16-bit BCD adder of **Fig. 2** can be extended to a 32-bit or 64-bit form with extra carry look ahead network levels.

A 64-bit BCD adder circuit includes three stages as discussed with reference to the 16-bit

- 10 adder **12** shown in **Fig. 2**. As shown in **Fig. 12**, Stage 1 has sixteen logic circuits **90, 92, ..., 118, 120** of the type identified by numeral **13** in **Fig. 3**.

The circuits **90-120** receive contiguous 4-bit operands **A[3:0]** and **B[3:0], A[7:4]** and **B[7:4]**, and so on, and generate respective intermediate sums **TS[3:0], ... TS[63:60]**, intermediate carries **TC3, ..., TC63**, propagate functions **P3-0, ..., P63-60**, and generate

- 15 functions **G3-0, ..., G63-60**.

The second stage carry look ahead circuits are shown in **Fig. 13**. Five carry look ahead circuits **130, 132, 134, 136, 138** are required. These circuits are of the same for as the circuit **17** shown in **Fig. 7**.

The carry look ahead circuits are in two sub-stages: four circuits **130, 132, 134, 136**

- 20 coupled with the first stage circuits **90-120** to receive 4-bit propagate and generate functions, and a single circuit **138**, receiving 16-bit propagate and generate functions from the first sub-stage. The outputs from the second sub-stage to the third stage are the carries **C16, C32, C48**, and **C64**.

The third stage, shown in **Fig. 14** has sixteen sum correction circuits **150, 152, ..., 178,**

- 25 **180**. Each of these circuits is implemented in the same manner as, for example, sum correction circuit **18** described with reference to **Figs. 8-11**. Together, the sum correction circuits **150-180** calculate **SUM[3:0]** to **SUM [63:60]** giving the sum result of the operands **A[63:0] + B[63:0] + C<sub>0</sub>**. The final carry is the value **C64**.

The 64-bit or 32-bit BCD adder requires six gate levels as shown in **Fig. 13** (circuits **130,**

- 30 **132, 134, 136** and **138**) in the second stage critical path.

The extension from 16-bit to 64-bit addition can be achieved with high reusability. A 64-bit adder circuit can be built by extending (i.e. reusing) the components of a 16-bit circuit four times, and adding only one extra level of a carry look ahead circuit.

*Conclusion*

- 5    The circuit described reduces the number of gate levels in the addition of two BCD-encoded operands with an input carry and makes the BCD addition fast.

While the invention contemplates equal length blocks for the operands, the embodiment taught is 4-bit blocks. For the 16-bit adder, the blocks are of contiguous bits from the

- 10   least to most significant bits. The use of 4-bit blocks is the most preferred, however, in that the fan-in and fan-out of carry look ahead logic is the least onerous to implement in hardware.

Various alterations and modifications can be made to the techniques and arrangements

- 15   described herein, as would be apparent to one skilled in the relevant art.